



Stacks and Queues

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CS 2401 (Fall 2010)

Elementary Data Structures and Algorithms

Two New ADTs

- ◆ Define two new abstract data types
 - ◆ Both are restricted lists
 - ◆ Can be implemented using arrays or linked lists
- ◆ Stacks
 - ◆ “Last In First Out” (LIFO)
- ◆ Queues
 - ◆ “First In First Out” (FIFO)

Stacks

- ◆ List of the same kind of elements
 - ◆ Addition and deletion of elements occur only at one end, called the top of the stack
- ◆ Computers use stacks to implement method calls
- ◆ Stacks are also used to convert recursive algorithms into nonrecursive algorithms

Conceptual Stacks

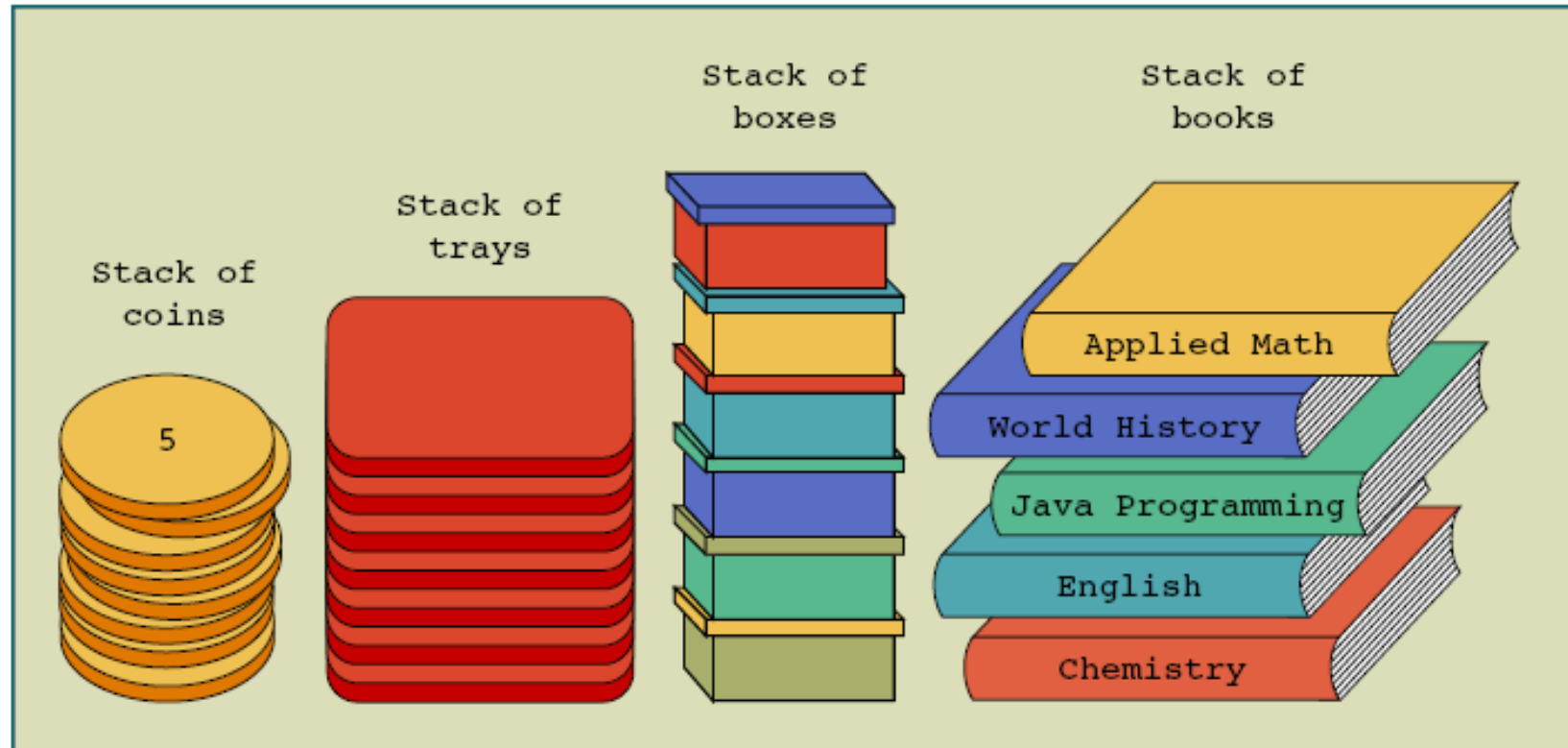


Figure 17-1 Various types of stacks

Stacks (continued)

- ◆ Stacks are also called Last Input First Output (LIFO) data structures
- ◆ Operations performed on stacks
 - ◆ Push: adds an element to the stack
 - ◆ Pop: removes an element from the stack
 - ◆ Peek: looks at the top element of the stack

Stacks (continued)

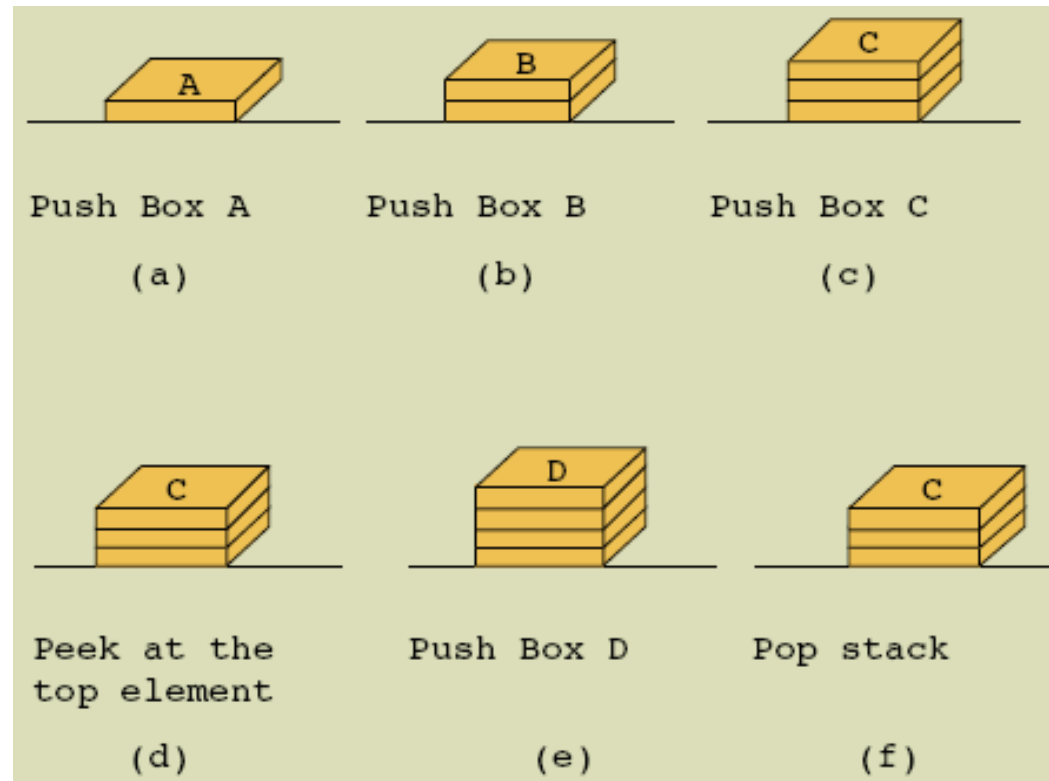


Figure 17-3 Stack operations

Stacks (continued)

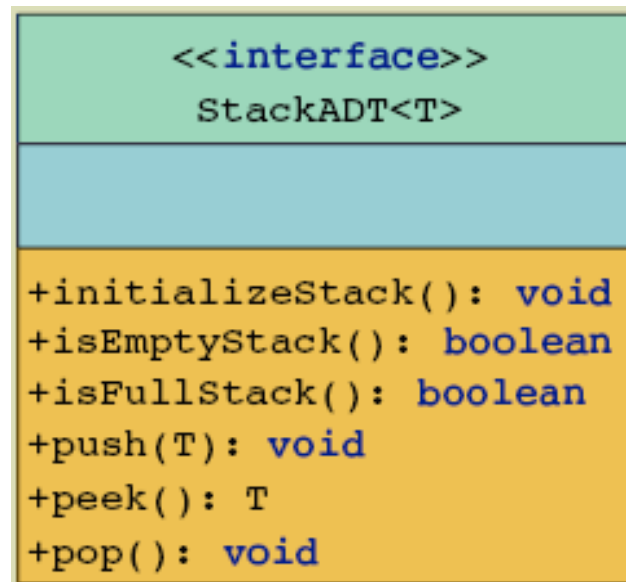


Figure 17-4 UML diagram of the `interface StackADT`

StackException Class

- ◆ Adding an element to a full stack and removing an element from an empty stack would generate errors or exceptions
 - ◆ Stack overflow exception
 - ◆ Stack underflow exception
- ◆ Classes that handle these exceptions
 - ◆ `StackException` extends `RuntimeException`
 - ◆ `StackOverflowException` extends `StackException`
 - ◆ `StackUnderflowException` extends `StackException`

Implementation of Stacks as Arrays

- ◆ The array implementing a stack is an array of reference variables
- ◆ Each element of the stack can be assigned to an array slot
- ◆ The top of the stack is the index of the last element added to the stack
- ◆ To keep track of the top position, declare a variable called `stackTop`

Implementation of Stacks as Arrays (continued)

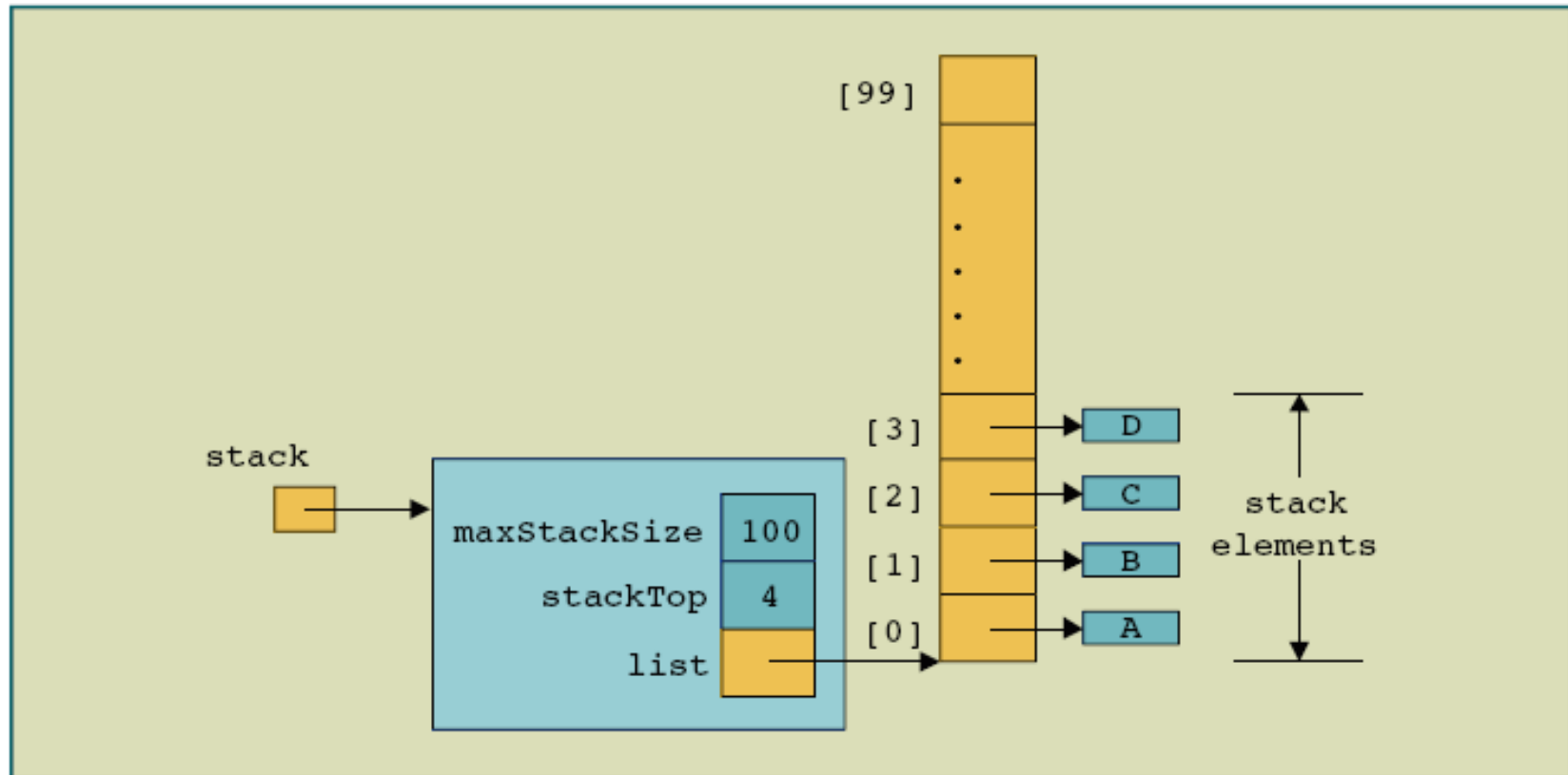


Figure 17-6 Example of a stack

Constructors

◆ Default constructor

```
public StackClass()  
{  
    maxStackSize = 100;  
    stackTop = 0;           //set stackTop to 0  
    list = (T[]) new Object[maxStackSize]; //create the array  
} //end default constructor
```

Initialize Stack

◆ Method initializeStack

```
public void initializeStack()
{
    for (int i = 0; i < stackTop; i++)
        list[i] = null;
    stackTop = 0;
} //end initializeStack
```

Empty Stack

- ◆ **Method isEmptyStack**

```
public boolean isEmptyStack()  
{  
    return (stackTop == 0);  
} //end isEmptyStack
```

Full Stack

◆ Method `isFullStack`

```
public boolean isFullStack()
{
    return (stackTop == maxStackSize);
} //end isFullStack
```

Push

◆ Method push

```
public void push(T newItem) throws StackOverflowException
{
    if (isFullStack())
        throw new StackOverflowException();
    list[stackTop] = newItem; //add newItem at the
                               //top of the stack
    stackTop++;               //increment stackTop
} //end push
```

Peek

◆ Method peek

```
public T peek() throws StackUnderflowException
{
    if (isEmptyStack())
        throw new StackUnderflowException();
    return (T) list[stackTop - 1];
} //end peek
```


Pop

◆ Method pop

```
public void pop() throws StackUnderflowException
{
    if (isEmptyStack())
        throw new StackUnderflowException();
    stackTop--;          //decrement stackTop
    list[stackTop] = null;
} //end pop
```

Linked Implementation of Stacks

- ◆ Arrays have fixed sizes
 - ◆ Only a fixed number of elements can be pushed onto the stack
- ◆ Dynamically allocate memory using reference variables
 - ◆ Implement a stack dynamically
- ◆ Similar to the array representation, `stackTop` is used to locate the top element
 - ◆ `stackTop` is now a reference variable

Linked Implementation of Stacks (continued)

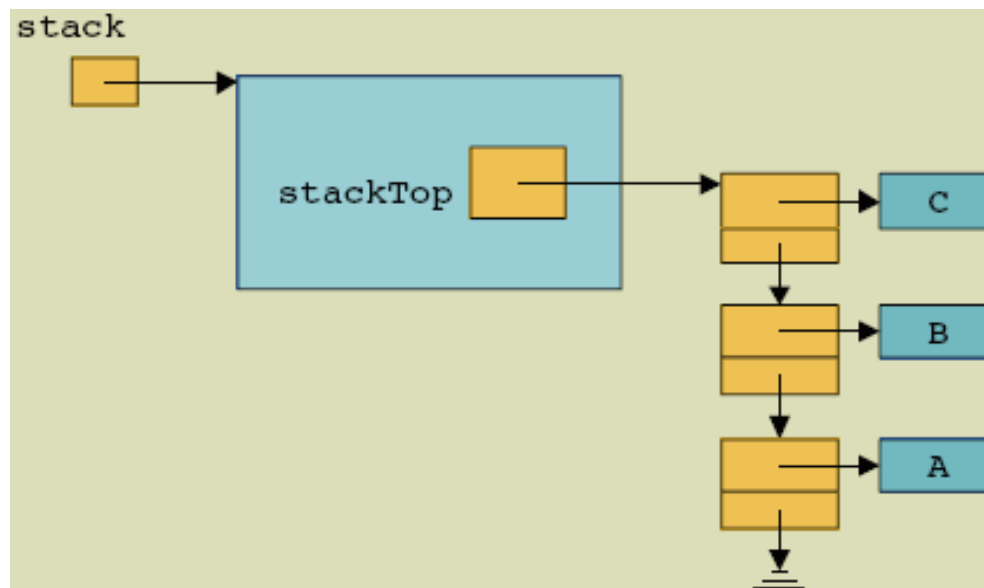


Figure 17-13 Nonempty linked stack

Default Constructor

◆ Default constructor

```
public LinkedStackClass()  
{  
    stackTop = null;  
} //end constructor
```

Initialize Stack

- ◆ **Method initializeStack**

```
public void initializeStack()  
{  
    stackTop = null;  
} //end initializeStack
```

Empty Stack and Full Stack

- ◆ **Methods isEmptyStack and isFullStack**

```
public boolean isEmptyStack()  
{  
    return (stackTop == null);  
} //end isEmptyStack
```

```
public boolean isFullStack()  
{  
    return false;  
} //end isFullStack
```

Push

◆ Method push

```
public void push(T newElement)
{
    StackNode<T> newNode; //reference variable to create
                          //the new node
    newNode = new
                StackNode<T>(newElement, stackTop); //create
                                                    //newNode and insert
                                                    //before stackTop
    stackTop = newNode; //set stackTop to point to
                       //the top element
} //end push
```

Peek

◆ Method peek

```
public T peek() throws StackUnderflowException
{
    if (stackTop == null)
        throw new StackUnderflowException();
    return stackTop.info;
} //end top
```


Pop

◆ Method pop

```
public void pop() throws StackUnderflowException
{
    if (stackTop == null)
        throw new StackUnderflowException();
    stackTop = stackTop.link; //advance stackTop to the
                               //next node
} //end pop
```

Applications of Stacks: Postfix Expression Calculator

- ◆ Infix notation
 - ◆ The operator is written between the operands
- ◆ Prefix or Polish notation
 - ◆ Operators are written before the operands
 - ◆ Does not require parentheses
- ◆ Reverse Polish or postfix notation
 - ◆ Operators follow the operands
 - ◆ Has the advantage that the operators appear in the order required for computation

Applications of Stacks: Postfix Expression Calculator (continued)

Infix Expression	Equivalent Postfix Expression
$a + b$	$a b +$
$a + b * c$	$a b c * +$
$a * b + c$	$a b * c +$
$(a + b) * c$	$a b + c *$
$(a - b) * (c + d)$	$a b - c d + *$
$(a + b) * (c - d / e) + f$	$a b + c d e / - * f +$

Table 17-1 Infix expressions and their equivalent postfix expressions

Applications of Stacks: Postfix Expression Calculator (continued)

- ◆ Algorithm to evaluate postfix expressions
 - ◆ Scan the expression from left to right
 - ◆ When an operator is found, back up to get the required number of operands
 - ◆ Perform the operation
 - ◆ Continue processing the expression

Main Algorithm

- ◆ Main algorithm in pseudocode for processing a postfix expression

```
Get the next expression
while more data to process
{
    a. initialize the stack
    b. process the expression
    c. output result
    d. get the next expression
}
```

Method evaluateExpression

◆ General algorithm for evaluateExpression

```
get the next token
while (token != '=')
{
    if (token is a number)
    {
        output number
        push number into stack
    }
    else
    {
        token is an operation
        call method evaluateOpr to evaluate the operation
    }
    if (no error in the expression)
        get next token
    else
        discard the expression
}
```

Method evaluateOpr

- ◆ This method evaluates an operation
- ◆ Two operands are needed to evaluate an operation
- ◆ Operands are stored in the stack
 - ◆ The stack must contain at least two operands
 - ◆ Otherwise, the operation cannot be evaluated

Removing Recursion: Nonrecursive Algorithm to Print a Linked List Backward

- ◆ Naïve approach
 - ◆ Get the last node of the list and print it
 - ◆ Traverse the link starting at the first node
 - ◆ Repeat this process for every node
 - ◆ Traverse the link starting at the first node until you reach the desired node
 - ◆ Very inefficient

Removing Recursion: Nonrecursive Algorithm to Print a Linked List Backward (continued)

```
current = first;           //Line 1
while (current != null)   //Line 2
{
    stack.push(current);   //Line 3
    current = current.link; //Line 4
}
```

Removing Recursion: Nonrecursive Algorithm to Print a Linked List Backward (continued)

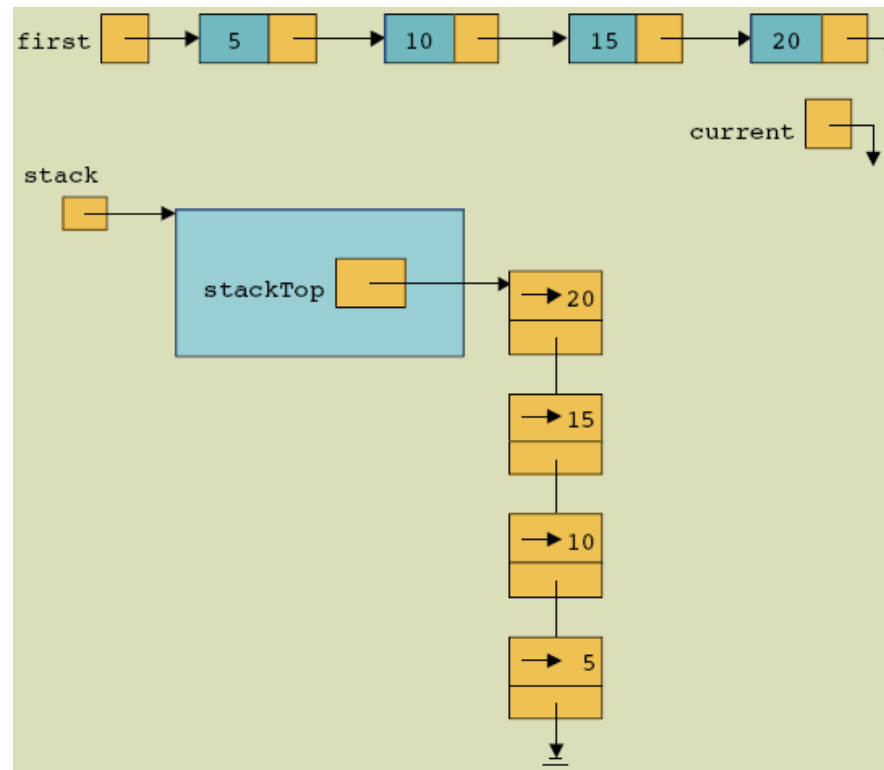


Figure 17-36 List and stack after the statements `stack.push(current);` and `current = current.link;` executes

The class Stack

```
public Stack()  
//Creates an empty Stack object.  
  
public boolean empty()  
//Returns true is the stack is empty; otherwise returns false.  
  
public Object peek() throws EmptyStackException  
//Returns the top element of the stack. It does not remove the  
//top element.  
  
public Object pop() throws EmptyStackException  
//Returns and removes the top element of the stack.  
  
public Object push(Object obj)  
//Pushes the item specified by obj onto the stack.  
  
public int search(Object obj)  
//Returns the relative position of the item specified by obj  
//from the top of the stack. If the item is not in the stack,  
//it returns -1.
```

Table 17-2 Members of the class Stack

Queues

- ◆ Data structure in which the elements are added at one end, called the rear, and deleted from the other end, called the front
- ◆ A queue is a First In First Out data structure
- ◆ As in a stack, the middle elements of the queue are inaccessible

Queue Operations

- ◆ Queue operations
 - ◆ `initializeQueue`
 - ◆ `isEmptyQueue`
 - ◆ `isFullQueue`
 - ◆ `front`
 - ◆ `back`
 - ◆ `addQueue`
 - ◆ `deleteQueue`

QueueException Class

- ◆ Adding an element to a full queue and removing an element from an empty queue would generate errors or exceptions
 - ◆ Queue overflow exception
 - ◆ Queue underflow exception
- ◆ Classes that handle these exceptions
 - ◆ `QueueException` extends `RuntimeException`
 - ◆ `QueueOverflowException` extends `QueueException`
 - ◆ `QueueUnderflowException` extends `QueueException`

Implementation of Queues as Arrays

- ◆ Instance variables
 - ◆ An array to store the queue elements
 - ◆ `queueFront` : keeps track of the first element
 - ◆ `queueRear` : keeps track of the last element
 - ◆ `maxQueueSize`: specifies the maximum size of the queues

Implementation of Queues as Arrays (continued)

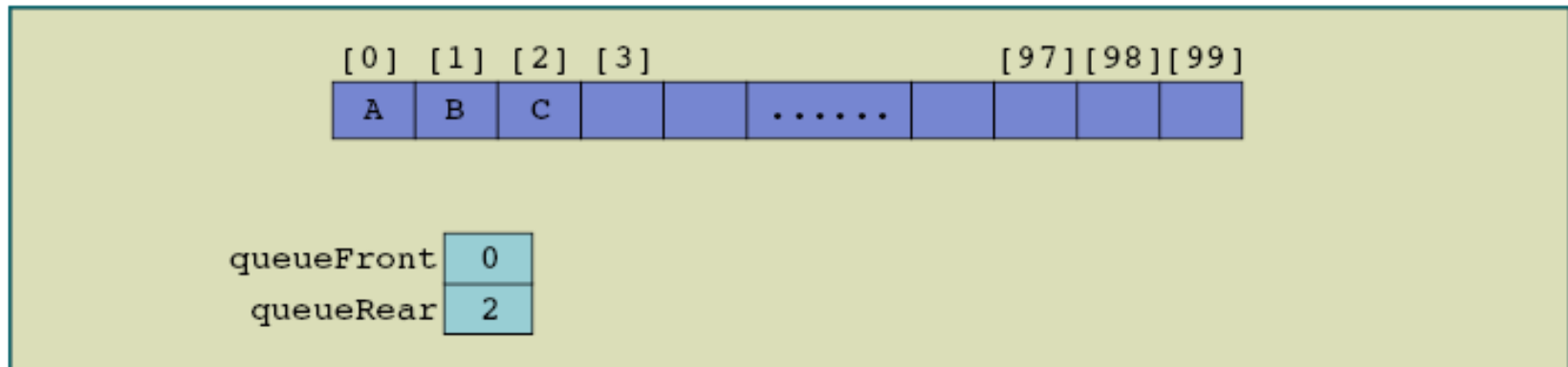


Figure 17-42 Queue after two more `addQueue` operations

Implementation of Queues as Arrays (continued)

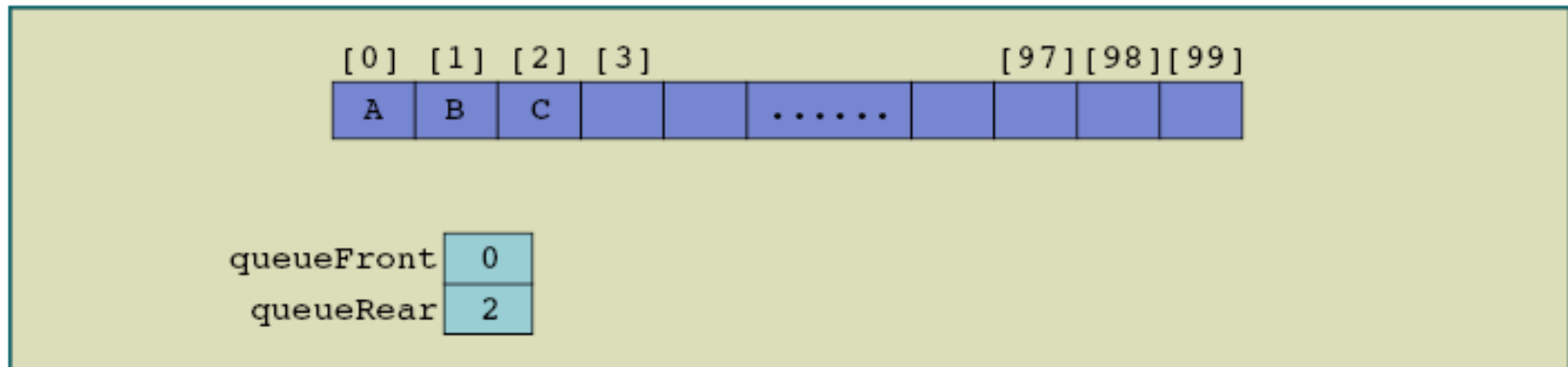


Figure 17-43 Queue after the `deleteQueue` operation

Implementation of Queues as Arrays (continued)

- ◆ Problems with this implementation
 - ◆ Arrays have fixed sizes
 - ◆ After various insertion and deletion operations, `queueRear` will point to the last array position
 - ◆ Giving the impression that the queue is full
- ◆ Solutions
 - ◆ Slide all of the queue elements toward the first array position
 - ◆ Use a circular array

Implementation of Queues as Arrays (continued)

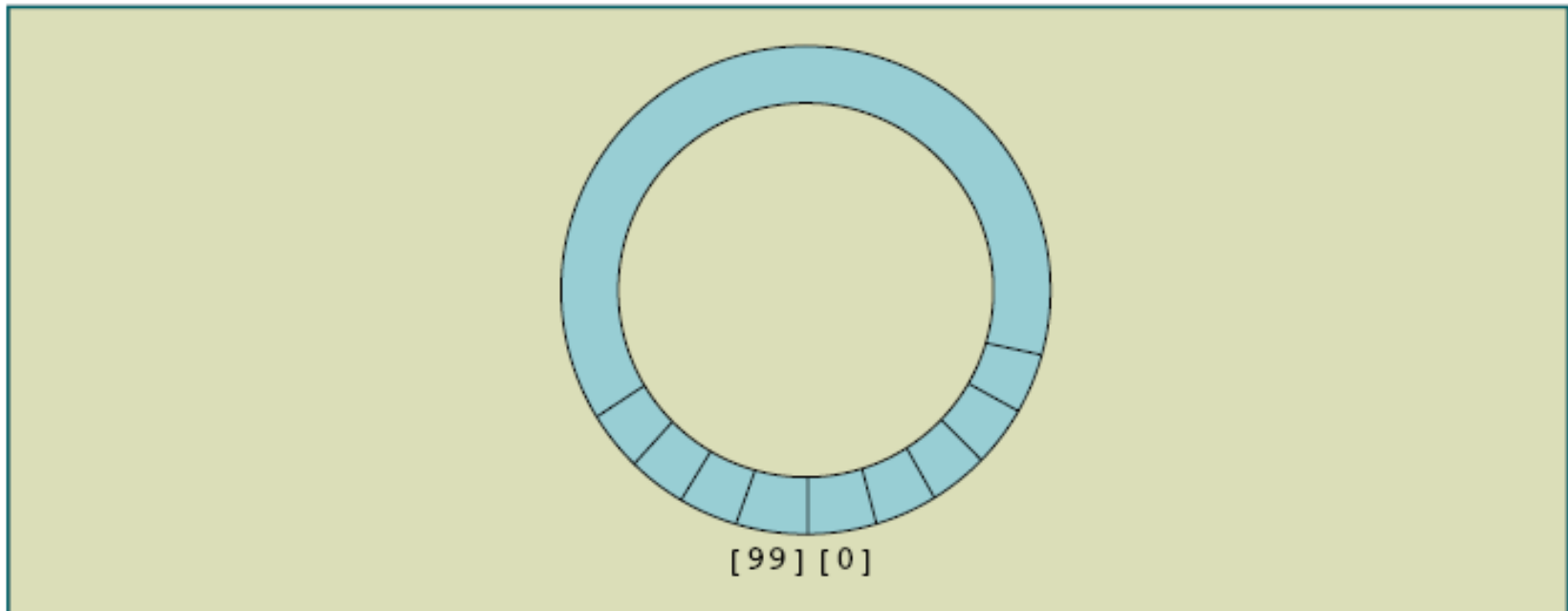


Figure 17-45 Circular queue

Implementation of Queues as Arrays (continued)

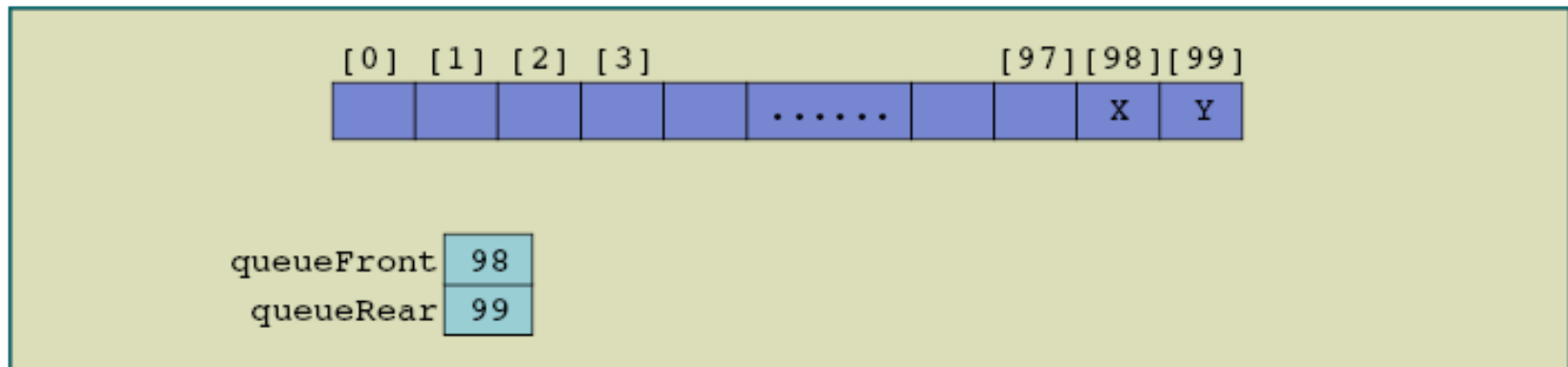


Figure 17-46 Queue with two elements at positions 98 and 99

Implementation of Queues as Arrays (continued)

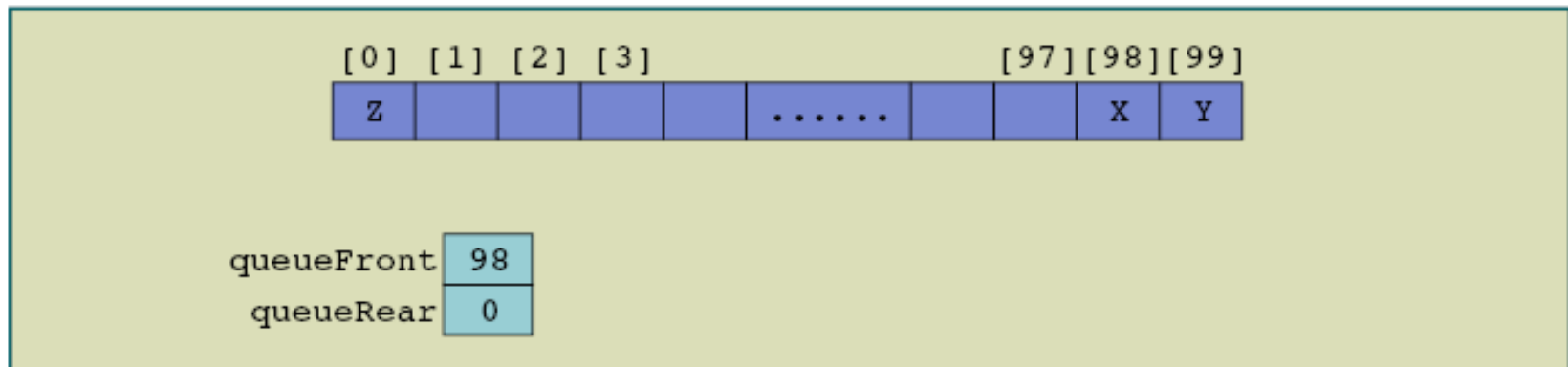


Figure 17-47 Queue after one more `addQueue` operation

Constructors

◆ Default constructor

```
//Default constructor
public QueueClass()
{
    maxQueueSize = 100;
    queueFront = 0;           //initialize queueFront
    queueRear = maxQueueSize - 1; //initialize queueRear
    count = 0;
    list = (T[]) new Object[maxQueueSize]; //create the
                                           //array to implement the queue
}
```

initializeQueue

◆ Method initializeQueue

```
public void initializeQueue()
{
    for (int i = queueFront; i < queueRear;
        i = (i + 1) % maxQueueSize)
        list[i] = null;
    queueFront = 0;
    queueRear = maxQueueSize - 1;
    count = 0;
}
```

Empty Queue and Full Queue

- ◆ **Methods isEmptyQueue and isFullQueue**

```
public boolean isEmptyQueue()  
{  
    return (count == 0);  
}
```

```
public boolean isFullQueue()  
{  
    return (count == maxQueueSize);  
}
```


Front

◆ Method front

```
public T front() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    return (T) list[queueFront];
}
```

Back

◆ Method back

```
public T back() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    return (T) list[queueRear];
}
```

addQueue

◆ Method addQueue

```
public void addQueue(T queueElement)
    throws QueueOverflowException
{
    if (isFullQueue())
        throw new QueueOverflowException();
    queueRear = (queueRear + 1) % maxQueueSize; //use the
        //mod operator to advance queueRear
        //because the array is circular
    count++;
    list[queueRear] = queueElement;
}
```

deleteQueue

◆ Method deleteQueue

```
public void deleteQueue() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    count--;
    list[queueFront] = null;
    queueFront = (queueFront + 1) % maxQueueSize; //use the
                                                    //mod operator to advance queueFront
                                                    //because the array is circular
}
```

Linked Implementation of Queues

- ◆ Simplifies many of the special cases of the array implementation
- ◆ Because the memory to store a queue element is allocated dynamically, the queue is never full
- ◆ Class `LinkedListClass` implements a queue as a linked data structure
 - ◆ It uses nodes of type `QueueNode`

Linked Implementation of Queues (continued)

- ◆ **Method initializeQueue**

```
public void initializeQueue()  
{  
    queueFront = null;  
    queueRear = null;  
}
```

Linked Implementation of Queues (continued)

- ◆ **Methods isEmptyQueue and isFullQueue**

```
public boolean isEmptyQueue()  
{  
    return (queueFront == null);  
}
```

```
public boolean isFullQueue()  
{  
    return false;  
}
```

addQueue

◆ Method addQueue

```
public void addQueue(T newElement)
{
    QueueNode<T> newNode;
    newNode = new QueueNode<T>(newElement, null); //create
                                                //newNode and assign newElement to newNode
    if (queueFront == null) //if initially the queue is empty
    {
        queueFront = newNode;
        queueRear = newNode;
    }
    else //add newNode at the end
    {
        queueRear.link = newNode;
        queueRear = queueRear.link;
    }
} //end addQueue
```


front and back

◆ Methods front and back

```
public T front() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    return queueFront.info;
}
```

```
public T back() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    return queueRear.info;
}
```

deleteQueue

◆ Method deleteQueue

```
public void deleteQueue() throws QueueUnderflowException
{
    if (isEmptyQueue())
        throw new QueueUnderflowException();
    queueFront = queueFront.link; //advance queueFront
    if (queueFront == null) //if after deletion the queue
        queueRear = null; //is empty, set queueRear to null
} //end deleteQueue
```