

(state of computer can be described by)

$S_{i,t}$ — state of i -th cell at t -th moment.

$S_{i,b,t}$ — b -th bit in i -th cell at t -th moment.

Tuesday

$c(x,y)$

comp. device

7th April

P_l

VP: x, y

Given: x

Find y s.t. $c(x,y) \& \text{len}(y) \leq P_l(\text{len}(x))$

O/P: T or F

Δt — time quantum

Δv — smallest size of the cell

(A cell can be any part of computer)

S — Largest # of states in a cell

$S_{i,t}$ — state of cell i at moment t

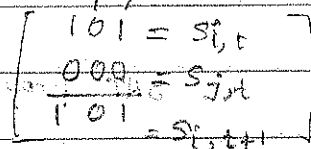
B — # of bits of to describe an individual state.

$$2^B \geq S = 2^{\log_2 S}$$

$$B \geq \log_2 S$$

$$B = \lceil \log_2 S \rceil$$

↳ smallest int $> \log_2 S$

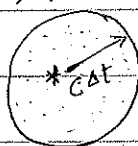


Example

$S_{i,t}$ consists of bit

$S_{i,b,t}$ be the b -th bit in the binary description of the state $S_{i,t}$.

$S_{i,t+1}$ depends on the state of different cells in prev moments of time.



distance traversed in $(t+1 - t = \Delta t)$ with speed of light (c)

$$= c \Delta t$$

max speed

$$N_{\text{neigh}} = \text{Neighbour of cells} \leq \frac{V}{\Delta v} = \frac{\frac{4}{3} \pi c^3 \Delta t^3}{\Delta v}$$

$$S_{i,t+1} = f_{i,t}(S_{i,t}, S_{j,t}) \rightarrow \text{so this means depends on bits describing states}$$

$\leq N_{\text{neigh}}$

$$S_{i,b,t+1} = f_{i,b,t}(S_{i,1,t}, S_{i,2,t}, \dots, S_{i,B,t}, \dots, S_{j,1,t}, \dots, S_{j,B,t})$$

CNF form:—

x_1, \dots, x_n } literals

$\bar{x}_1, \dots, \bar{x}_n$ }

AND
 $(x_1 \vee x_2) \& (x_1 \vee x_3)$

CNF form.

By truth table, we can convert to CNF form.

$$f(x_1, x_2) \equiv (x_1 = x_2)$$

x_1	x_2	f	$f \equiv (\bar{x}_1 \wedge \bar{x}_2) \vee (x_1 \wedge x_2)$ $\neg f \equiv (\bar{x}_1 \wedge x_2) \vee (x_1 \wedge \bar{x}_2)$ De Morgan's law: $\neg(a \wedge b) \equiv \neg a \vee \neg b$ $\neg(a \vee b) \equiv \neg a \wedge \neg b$	} DNF
F	F	T		
F	T	F		
T	T	T		

$$f \equiv \neg[\neg f] \equiv \neg[(\bar{x}_1 \wedge x_2) \vee (x_1 \wedge \bar{x}_2)]$$

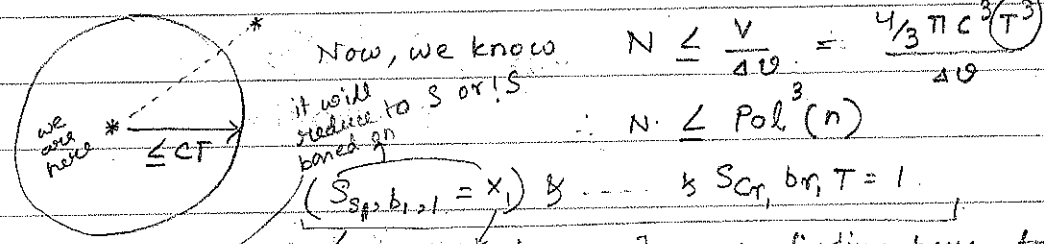
$$\equiv \neg(\bar{x}_1 \wedge x_2) \wedge \neg(x_1 \wedge \bar{x}_2)$$

$$\equiv (x_1 \vee \bar{x}_2) \wedge (\bar{x}_1 \vee x_2) \quad \text{--- CNF}$$

$$F_{1,1} \wedge F_{1,2} \wedge \dots \wedge F_{N,B,T} \wedge \dots$$

Formula showing transition from 1st bit at 1st moment at first cell. Computational time of $c(x, y)$ another polynomial.

$$T \leq P_c(\text{len}(x) + \text{len}(y)) \leq P_2(n)$$



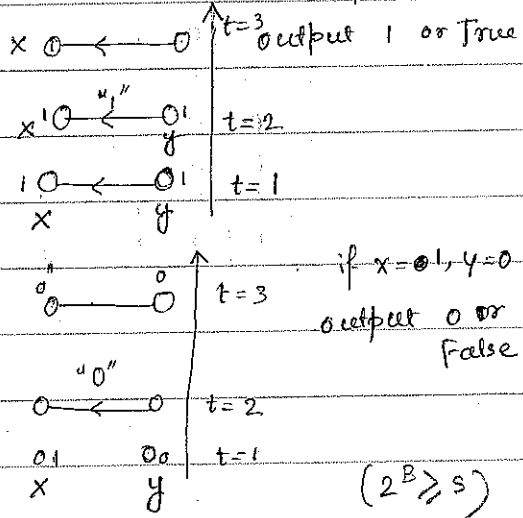
$$S=1 \equiv S$$

$$S=0 \equiv !S$$

input is x_i we are finding here for which $x, c_{x,y} = 1$. So, we can find value of x , for which $c_{x,y} = 1$, if we can solve this in polynomial time.

So, we have reduced to this propositional logic time if $x=1, y=1$

Example:- x - 1 bit
 y - 1 bit
 $c(x, y) \equiv (x = y)$ equals



So, here we have 3 cells x, y , the wire carrying wire $N=3$
 states x can have = 2
 y " " = 2.
 wire " " = 3 states.
 (No signal, 0, 1)

∴ Max no of state = 3 ∴ no of bits to represent 3 state = 2

Represent states with bits

(see picture)

cell x : 00 01

For cell x. $S_{112} = S_{111} = 0$ f_{111}

cell y : 00 01

$S_{122} = S_{121}$ f_{121}

wire : no signal 00

For cell y. $S_{212} = 0$

"signal 0" 10

$S_{222} = S_{221}$

"signal 1" 11

For wire. $S_{312} = 1$

f_{111} & f_{121} ... & f_{322}

$S_{322} = S_{221}$ f_{322}

$$= \neg S_{112} \& (\bar{S}_{122} \vee S_{121}) \& (S_{122} \vee \bar{S}_{121}) \& \neg S_{212} \& (\bar{S}_{222} \vee S_{221}) \& (\bar{S}_{221} \& S_{222}) \& \bar{S}_{312} \& (\bar{S}_{322} \vee S_{221}) \vee (S_{223} \vee \bar{S}_{222}) \& (\bar{S}_{223} \vee S_{222}) \& \bar{S}_{313} \& \bar{S}_{323} \& \bar{S}_{113} \& (S_{123} \vee S_{322} \vee S_{122})$$

... = result is true.

For 3rd state (x)

* $S_{213} = 0$

$S_{223} = S_{222}$

$S_{313} = 0$

$S_{323} = 0$

$S_{113} = 0$

$S_{123} = \begin{cases} 1 & \text{if } S_{322} = S_{122} \\ 0 & \text{otherwise} \end{cases}$

$a = \begin{cases} 1 & \text{if } b=c \\ 0 & \text{otherwise} \end{cases}$ $b=c \& a=1$ then true.
 $\hookrightarrow b \neq c \& a=0$ then true.

a	b	c	f	F
0	0	0	0	1
0	0	1	1	0
0	1	0	0	1
0	1	1	1	0
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	0
0	1	1	0	1

$$F = [(\bar{a} \& \bar{b} \& \bar{c}) \vee (\bar{a} \& b \& c) \vee (a \& \bar{b} \& c) \vee (a \& b \& \bar{c})]$$

$$f = (a \vee b \vee c) \wedge (\bar{a} \vee \bar{b} \vee \bar{c})$$

 * $(\bar{a} \vee b \vee \bar{c}) \wedge (\bar{a} \vee \bar{b} \vee c)$

H.W. checking if $x \rightarrow y$
 \downarrow
 $\neg x \vee y$