

Solution to Homework Problem 17

Task. Use the general algorithm to transform a finite automaton B from Homework 1.4 – as simplified in Homework 3, into a Turing machine. Show step-by-step, on an example of a word 1a, how this word will be processed by your Turing machine.

Automaton B from Homework 1.4 as simplified in Homework 3: reminder. This automaton has two states: n and w ; n is the starting state, and it is also the only final state. The transitions are as follows:

- from the state n , symbol 1 leads to n , every other symbol leads to w ;
- from the state w , every symbol leads back to w .

Solution. Here are the rules for the Turing machine:

start, $- \rightarrow R, n$
 $n, 1 \rightarrow R, n$
 $n, a \rightarrow R, w$
 $n, ? \rightarrow R, w$
 $w, 1 \rightarrow R, w$
 $w, a \rightarrow R, w$
 $w, ? \rightarrow R, w$
 $n, - \rightarrow \text{accept}$
 $w, - \rightarrow \text{reject}$

Tracing.

-	1	a	-	-	...	start
-	<u>1</u>	a	-	-	...	n
-	1	<u>a</u>	-	-	...	n
-	1	a	-	-	...	w
-	1	a	-	-	...	reject