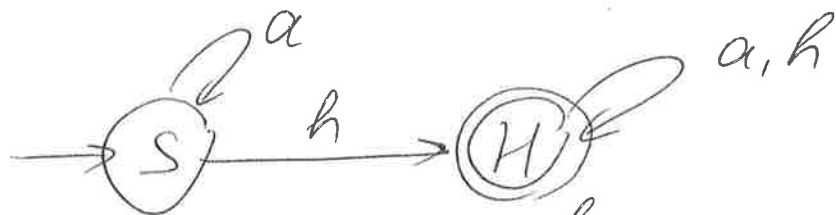
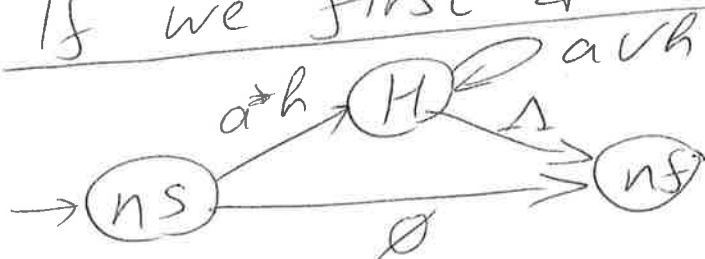


HW3
pt.1



If we first delete S:



$$R'_{ns, H} = R_{ns, H} \cup (R_{ns, S} R_{S, S}^+ R_{S, H}) = \emptyset \cup (\Lambda a^* h) = a^* h$$

$$R'_{ns, nf} = R_{ns, nf} \cup (R_{ns, S} R_{S, S}^+ R_{S, nf}) = \emptyset \cup (\Lambda a^* \emptyset) = \emptyset$$

$$R'_{H, H} = R_{H, H} \cup (R_{H, S} R_{S, S}^+ R_{S, H}) = a \cup h \cup (\emptyset \dots) = a \cup h$$

$$R'_{H, nf} = R_{H, nf} \cup (R_{H, S} R_{S, S}^+ R_{S, nf}) = \Lambda \cup (\emptyset \dots) = \Lambda$$

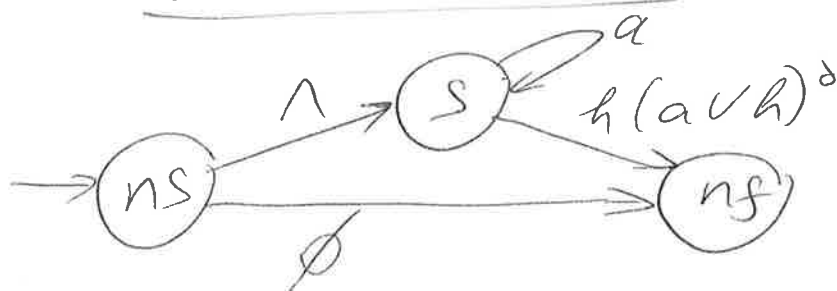


$$R'_{ns, nf} = R_{ns, nf} \cup (R_{ns, H} R_{H, H}^+ R_{H, nf}) = \emptyset \cup (a^* h (a \cup h)^+ \Lambda) = \underline{a^* h (a \cup h)^*}$$

HW3

pt. 2

If we delete H,

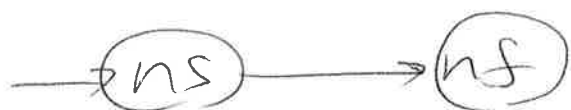


$$R'_{ns,s} = R_{ns,s} \cup (R_{ns,H} R_{H,H}^* R_{H,s}) = \Lambda \cup (\phi \dots) = \Lambda$$

$$R'_{ns,nf} = R_{ns,nf} \cup (R_{ns,H} R_{H,H}^* R_{H,nf}) = \phi \cup (\phi \dots) = \phi$$

$$R'_{s,s} = R_{s,s} \cup (R_{s,H} R_{H,H}^* R_{H,s}) = a \cup (h(a \vee h)^* \phi) = a$$

$$R'_{s,nf} = R_{s,nf} \cup (R_{s,H} R_{H,H}^* R_{H,nf}) = \phi \cup (h(a \vee h)^* \Lambda) = h(a \vee h)^*$$



$$R'_{ns,nf} = R_{ns,nf} \cup (R_{ns,s} R_{s,s}^* R_{s,nf}) = \phi \cup (\Lambda a^* (h(a \vee h)^*)^*) = \underline{a^* (h(a \vee h)^*)^*}$$