

$$m_A(n) = \begin{cases} 1 & \text{if } n \in A \\ 0 & \text{otherwise} \end{cases} \quad \Bigg\| \text{decidable.}$$

Semidecidable:

$$m_A(n) = \begin{cases} 1 & \text{if } n \in A \\ \emptyset & \text{if } n \notin A \end{cases}$$

↓
(runs indefinitely)

- + If A is r.e. \rightarrow then A is \emptyset semi-decidable
- Have an algorithm that prints all elements in A .

$m_A(n)$ waits and checks every hour whether n was printed.

halts.
 \rightarrow true (1) $\rightarrow n \in A$
 \rightarrow runs indefinitely $\rightarrow m_A(n)$

- + If A is semi-decidable then A is r.e.

b 26, 09

Review: μ recursive implementation on TM

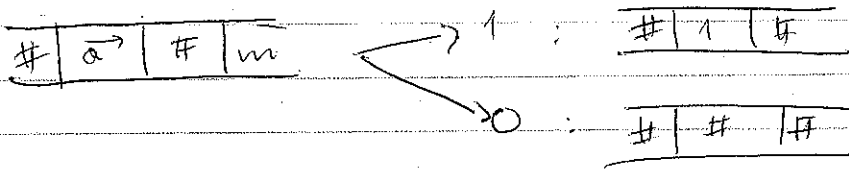
Big Pic: μ recursive f.n.
 \downarrow
 TM

Proving that every μ .rec. f.n. is Turing computable!

\emptyset, σ, π by \emptyset (PR) μ recursion

$\mu_m \times P(\vec{a}, m) = f(\vec{a})$
 // while \rightarrow no condition to stop

We know $P(a^{\rightarrow}, m)$ is Turing computable



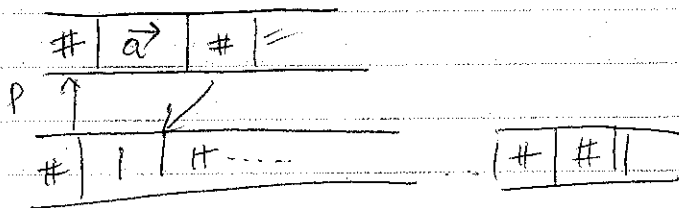
We wanna produce a TM for computing.

Analyze the problem.

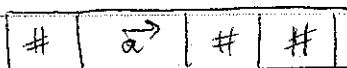
Idea: try $m=0$
 if $P(a^{\rightarrow}, 0)$ return 0;
 else
 try $m=1$
 if $P(a^{\rightarrow}, 1)$ return 1;

```

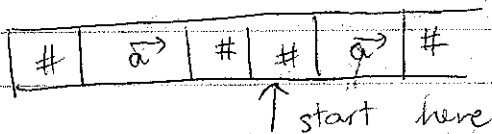
m = 0
while (!P(a^>, m))
{
    m++;
}
    
```



* correct way:



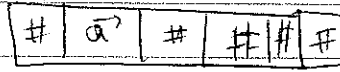
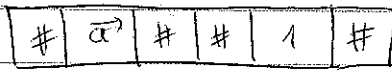
copy a^{\rightarrow}



$p(a^2, 0)$
is true

Result

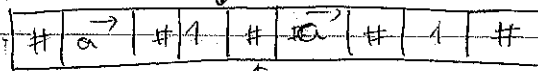
$p(a^2, 0)$
is false



$m+1$

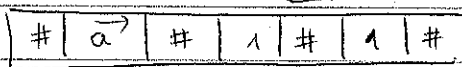


copy



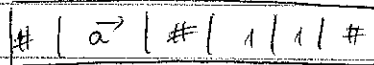
$p(a^2, 1)$
is true

$p(a^2, 1)$ is false



return 1
 π_{k+1}^{k+2}

$m+1$

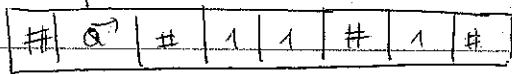


copy



$p(a^2, 2)$ is true

false



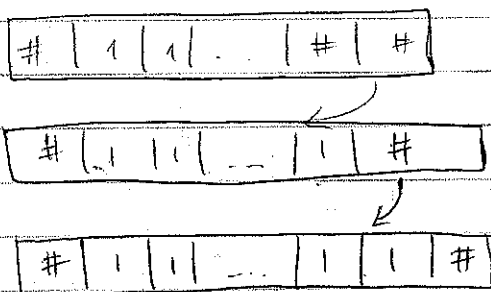
return 2 = π_{k+1}^{k+2}

Big problem with what we had so far.

+ when we had a negative result, it was OK.

+ sometimes, actually produced algorithms, but many of these algorithms were unrealistically long.

Example: $\sigma(n) = n + 1$.

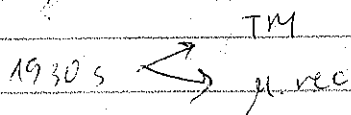


For security, we have integers: 160-200 digit long.

10^{100} impossible # of steps.

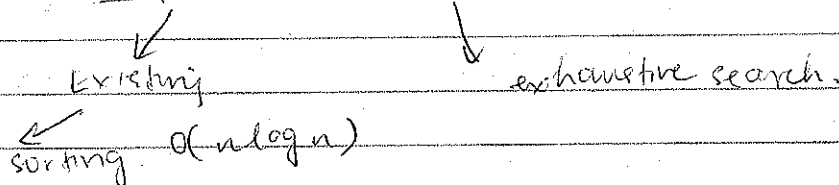
→ we need to separate "theoretical" algorithms from practical algorithms.
feasible.

+ How do you define an algorithm?



+ How do you define a feasible algorithm?

No perfect definition exists.



A little bit of physics

$$1 \text{ year} = 365 \text{ days} = 3 \times 10^7 \frac{\text{seconds}}{\text{year}}$$

$$\begin{aligned} T &= 20 \text{ billion years} \\ &\approx 2 \times 10^{10} \text{ years} \\ &= 6 \times 10^{17} \text{ seconds} \end{aligned}$$

$$\Delta t = \frac{\text{dist}}{\text{velo.}}$$

T

$\Delta t \leftarrow$ smallest possible time interval

$t =$ time during which the light goes through the smallest elementary particle.

Heisenberg's uncertainty principle.

$$\Delta x \Delta p \geq \frac{h}{2\pi} \quad h = \text{planck's constant}$$

Q Next Thursday : Quiz / Test.