Solution to Problem 18

Problem. Suppose that $A$, $B$ are r.e. sets. If a number $n$ appears in the $A$-generating algorithm at moment 4, when will this number appear in the algorithm generating all elements of the union $A \cup B$?

Solution. According to the posted lecture, if the $A$-generating algorithm generates a number at moment $k$, then the union-generating algorithm generates this number at moment $2k - 1$.

In this problem, $k = 4$, so the union-generating algorithm generates the number $n$ at moment $2 \cdot 4 - 1 = 7$. 