

f

$\tilde{x}_1, \tilde{x}_2, \dots, \tilde{x}_n$

```
public double partialDeriv(double[] tildeX, int i, double h){
    double tilde y = f(tilde x);
    double[]
    int n = tilde x.length;
    double[] x-mod = new double[n];
    for(j=0; j<n; j++){
        x-mod[j] = tilde x[j];
        x-mod[i] += h;
        double y-mod = f(x-mod);
        return (y-mod - y-tilde)/h;
    }
}

public double f(double[] x){
    double sum = 0.0;
    for(int i=0; i<x.length; i++){
        sum += x[i];
    }
    return sum;
}
```

Thurs Sept 25th - preview of the test

Tue Sept 30th - test.

Thurs Oct 2nd - work on your project day.

Tue Oct 6th - Report.

Mon Sept 29th.

Additional part:

R. Bafer Kearfott -

10³⁰ - 11²⁰ pm

TRCR

Friday, 12 pm. - post-conf workshop

Templeton suite

Sat - Oct 5 until noon

NSF

Problem:

we have: $f(x_1, x_2, \dots, x_n)$

$\tilde{x}_1, \tilde{x}_2, \dots, \tilde{x}_n$

$\sigma_1, \sigma_2, \dots, \sigma_n$.

We want: $\tilde{y}, \sigma \rightarrow$ we want.

Algorithm:

$$\sigma = \sqrt{\sum_{i=1}^n (f(x_1, \dots, x_{i-1}, x_i + \sigma_i, x_{i+1}, \dots, x_n) - \tilde{y})^2}$$

We did: small n

- we used numerical differentiation as main tool.
- we used simulations (which run much longer) to check on results.

Monte Carlo Simulations:

$$\tilde{y} = f(\tilde{x}_1, \dots, \tilde{x}_n)$$

Fix some no of iterations N

for each iteration $k=1, \dots, N$

* simulate meas. errors $\Delta x_i^{(k)} = \sigma_i * \text{gauss}()$;

* simulate the actual values $x_i^{(k)} = \tilde{x}_i - \Delta x_i^{(k)}$

* simulate y ; $y^{(k)} = f(x_1^{(k)}, \dots, x_n^{(k)})$

* simulate $\Delta y^{(k)} = \tilde{y} - y^{(k)}$

$$\sigma = \sqrt{\frac{1}{N} \sum_{k=1}^N (\Delta y^{(k)})^2}$$

$$\text{Accuracy} \approx \frac{1}{\sqrt{N}}$$

3%, $N=1000$

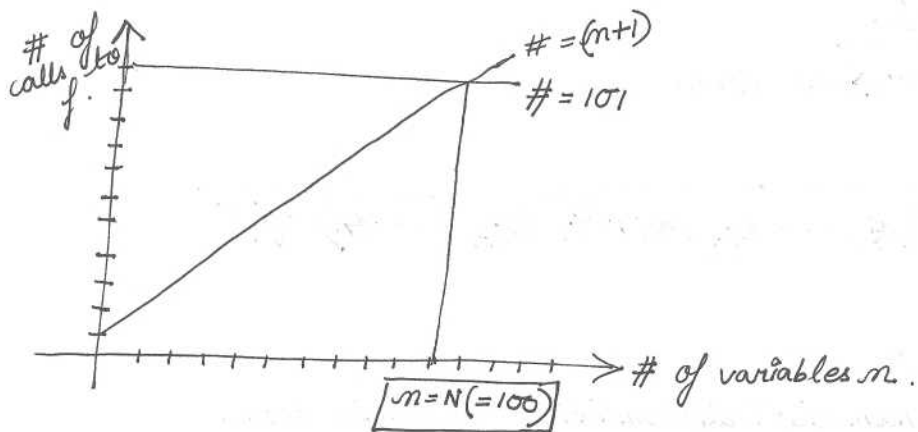
10%, $N=100$

HW: To write a program to generate σ using Monte-Carlo method.

Main time : computing f .

numerical diff : $(n+1)$ calls to f .

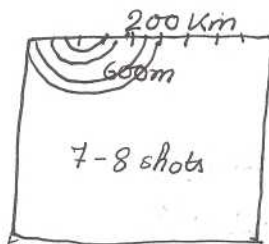
Monte - Carlo : $(N+1)$ calls to f .



If we have ~~var~~ # of variables $> N \Rightarrow$ Monte Carlo

" " " " " $< N \Rightarrow$ numerical diff

Geosciences Experiment:



$$300 \cdot 7 = 2100$$

Optimal Curve:

