

# Why Fuzzy Techniques in Explainable AI? Which Fuzzy Techniques in Explainable AI?

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## 1. Need for Explainable AI

- Lately, there have been a breakthrough in AI caused by successes of deep learning.
- Deep learning techniques have been very successful in many applications.
- However, serious problems surfaced.
- The main problem is that a trained neural network is a black box, it does not provide any explanations.
- Since no tool is 100% accurate, it is not clear how to separate correct advice from wrong advice.
- In social situations, the advice can be very wrong, repeating the biases of the training data.
- It is therefore desirable to develop AI tools that would:
  - translate numerical recommendations
  - into natural-language explanations.

## 2. Why Fuzzy in Explainable AI

- We want to translate numerical recommendations into natural-language descriptions.
- It is reasonable to utilize *fuzzy* techniques that:
  - have been designed in the 1960s – and successfully used since then,
  - to relate natural-language descriptions and numerical recommendations.
- In these techniques:
  - to each expert statement and to each propositional combination of expert statements,
  - we assign *a degree of confidence*,
  - i.e., a number from the interval  $[0, 1]$  describing to what extent we are confident in a given statement.

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### 3. Which Fuzzy Techniques in Explainable AI

- There are many different versions of fuzzy techniques.
- The main idea is that there are many different “and” and “or”-operations.
- These are functions  $f_{\&}(a, b)$  and  $f_{\vee}(a, b)$  that:
  - estimate our degrees of certainty in statements  $A \& B$  and  $A \vee B$
  - in situations in which we only know the degrees of confidence  $a$  and  $b$  in the statements  $A$  and  $B$ .
- These operations are also known as t-norms and t-conorms.
- It is known that a wrong choice of an operation can hinder the effectiveness of the resulting system.
- So which operations should we choose?

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## 4. Two Types of Situations

- In this talk, we will consider two types of situations:
- In some cases, we are interested in the best performance of an individual system.
- For example, we have a single drone performing meteorological (or other) observations.
- We want to make sure that its probability of failure is as small as possible.
- In other cases, we have a mass phenomenon; e.g.:
  - we are controlling a swarm of drones,
  - or a large number of local power stations contributing to the same grid.

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## 5. Two Types of Situations (cont-d)

- In this case:
  - we can afford the failure of some of these objects and thus, use less expensive equipment
  - if this allows us to have more objects and attain the best overall performance.
- We will show that in these two types of situations, different “and”- and “or”-operations are preferable.

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## 6. Situations Where We Are Interested in the Individual Performance

- In such situations:
  - we want to minimize the probability of failure,
  - we want the deviations of the object from the desired trajectory to be as small as possible,
  - since it is such deviations that cause failure.
- What are the possible reasons for such deviations in fuzzy control?
- Fuzzy control is based on:
  - combining the original experts' degree of confidence
  - by using “and”- and “or”-operations.

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## 7. Individual Performance (cont-d)

- The original estimates are only provided with some uncertainty:
  - just like an expert cannot provide the exact value of the desired control,
  - this is why fuzzy techniques are needed in the first place,
  - the expert also cannot describe his/her degree of confidence in a statement by an exact number.
- If we force the expert to do it – as many systems do:
  - the expert will provide slightly different numbers
  - when asked again about the same statements.
- These changes affect the results of “and”- and “or”-operations – and thus, affect the resulting control.

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## 8. Individual Performance (cont-d)

- A single too-large deviation from the desired control can be disastrous.
- So, to be on the safe side, we want to make sure that the worst-possible deviation is as small as possible.
- Let us describe this situation in precise terms.
- Let  $\delta > 0$  denote the accuracy with which the experts can provide their degrees.
- This means that for a statement  $A$ , the same expert:
  - can provide different estimates  $a$  and  $a'$  for his/her degree of confidence in  $A$ ;
  - these estimates are  $\delta$ -close:  $|a - a'| \leq \delta$ .
- Similarly, for another statement  $B$ , the expert can provide estimates  $b$  and  $b'$  for which  $|b - b'| \leq \delta$ .

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## 9. Individual Performance (cont-d)

- As a result of this uncertainty, we can have different values  $f_{\&}(a, b)$  and  $f_{\&}(a', b')$ :

$$|f_{\&}(a, b) - f_{\&}(a', b')| \neq 0.$$

- The worst-case scenario is when this difference is the largest possible.
- It is characterized by the value

$$w(f_{\&}, \delta) \stackrel{\text{def}}{=} \max_{|a-a'| \leq \delta, |b-b'| \leq \delta} |f_{\&}(a, b) - f_{\&}(a', b')|.$$

- We want to select an “and”-operation for which this worst-case value is the smallest possible.
- It is known that in this case, the optimal “and”-operation is  $f_{\&}(a, b) = \min(a, b)$ .
- Similarly, for an “or”-operation, the corresponding difference has the form  $|f_{\vee}(a, b) - f_{\vee}(a', b')|$ .

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## 10. Individual Performance (cont-d)

- So, the worst-case scenario is when this difference is the largest possible.
- It is characterized by the value

$$w(f_{\vee}, \delta) \stackrel{\text{def}}{=} \max_{|a-a'| \leq \delta, |b-b'| \leq \delta} |f_{\vee}(a, b) - f_{\vee}(a', b')|.$$

- We want to select an “or”-operation for which this worst-case value is the smallest possible.
- It turns out that in this case, the optimal “or”-operation is  $f_{\vee}(a, b) = \max(a, b)$ .
- So:

- in situations when we are interested in the individual performance,
- the optimal selection of fuzzy operations is

$$f_{\&}(a, b) = \min(a, b) \text{ and } f_{\vee}(a, b) = \max(a, b).$$

## 11. Situations Where We Are Interested in the Group Performance

- In such situations, we may allow some systems to fail.
- We would like to minimize the number of failing systems – i.e., the probability that a system will fail.
- A system fails if the corresponding parameters deviate too much from their desired values.
- Each of these parameters is affected by many different factors.
- It is known that:
  - under reasonable conditions,
  - the distribution of the joint effect of many independent factors is close to Gaussian.
- This is known as the Central Limit Theorem.

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## 12. Group Performance (cont-d)

- A normal distribution of each quantity  $y$  is uniquely determined by its mean and by its standard deviation.
- Usually, we can safely assume that the mean is 0 (or close to 0).
- For a normal distribution with 0 mean and standard deviation  $\sigma$ :
  - the probability of exceeding a threshold value  $x_0$
  - depends only on the ratio  $x_0/\sigma$ .
- The larger this ratio – i.e., equivalently, the smaller  $\sigma$ 
  - the smaller this probability.

### 13. Group Performance (cont-d)

- In general, for a function  $y = f(x_1, \dots, x_n)$  of several variables:
  - when the change  $\Delta x_i$  is small,
  - the corresponding change in  $\Delta y$  is approximately equal to  $\frac{\partial f}{\partial x_i} \cdot \Delta x_i$ ;
  - thus, the corresponding variance  $\sigma^2$  of  $y$  is approximately equal to

$$\left(\frac{\partial f}{\partial x_i}\right)^2 \cdot (\sigma_i)^2;$$

- here  $\sigma_i$  is the standard deviation of  $\Delta x_i$ .
- Thus, to minimize  $\sigma$ , we need to minimize all the values  $\sigma_i$  as well.

## 14. Group Performance (cont-d)

- In particular:
  - for the result  $c = f_{\&}(a, b)$  of an “and”-operation,
  - this means that we need to minimize the standard deviation caused by random deviations  $\Delta a$  and  $\Delta b$ .
- For small deviations, for each  $a$  and  $b$ , we have

$$\Delta c = \frac{\partial f_{\&}(a, b)}{\partial a} \cdot \Delta a + \frac{\partial f_{\&}(a, b)}{\partial b} \cdot \Delta b.$$

- The natural assumption is that the deviations  $\Delta a$  and  $\Delta b$  are i.i.d., with standard deviation  $\sigma_0$ .
- Then, we get

$$\sigma^2(a, b) = \left( \frac{\partial f_{\&}(a, b)}{\partial a} \right)^2 \cdot \sigma_0^2 + \left( \frac{\partial f_{\&}(a, b)}{\partial b} \right)^2 \cdot \sigma_0^2.$$

## 15. Group Performance (cont-d)

- The overall standard deviation can be obtained by averaging this value over all possible  $a$  and  $b$ :

$$\sigma^2 = \int \sigma^2(a, b) da db =$$

$$\int \left( \left( \frac{\partial f_{\&}(a, b)}{\partial a} \right)^2 \cdot \sigma_0^2 + \left( \frac{\partial f_{\&}(a, b)}{\partial b} \right)^2 \cdot \sigma_0^2 \right) da db.$$

- Thus, minimizing the standard deviation means minimizing this integral.
- It turns out that the “and”-operation  $f_{\&}(a, b)$  for which this integral is the smallest possible is  $f_{\&}(a, b) = a \cdot b$ .



## 16. Group Performance (cont-d)

- Similarly, for the “or”-operation, we need to minimize the integral

$$\sigma^2 = \int \left( \left( \frac{\partial f_{\vee}(a, b)}{\partial a} \right)^2 \cdot \sigma_0^2 + \left( \frac{\partial f_{\vee}(a, b)}{\partial b} \right)^2 \cdot \sigma_0^2 \right) da db.$$

- It is known that the “or”-operation  $f_{\vee}(a, b)$  for which this integral is the smallest possible is

$$f_{\vee}(a, b) = a + b - a \cdot b.$$

- So, in situations when we are interested in the group performance, the optimal fuzzy operations are:

$$f_{\&}(a, b) = a \cdot b \text{ and } f_{\vee}(a, b) = a + b - a \cdot b.$$

## 17. Other Possible Situations

- We may be looking for the operations:
  - that lead to the smoothest trajectory, or
  - that lead to the most stable control, or
  - which are the fastest to compute.
- In all these cases, we end up with different pairs of optimal “and”- and “or”-operations.

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