# Why Cyberattacks Are Easier Than Cyberdefense

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## 1. Formulation of the problem

- In general, in military confrontations, defense is easier than an attack.
- However, in cybersecurity, the inverse is true: cyberattacks are easier than cyberdefense.
- Many times:
  - college kids who have not yet finished their education
  - managed to penetrate sophisticated cybersecurity arrangements of Pentagon and other heavily protected targets.
- How can we explain this?

# 2. Our explanation

- For each system s and attack a, let S(a, s) indicate that the attack a was successful against the system s.
- For each pair a and s, it is feasible to check whether S(a, s) is true.
- To check this, it is sufficient to launch the attack and see if it succeeds.
- In other words, the predicate S(a, s) is feasible: its truth value can be computed by a feasible (= time-polynomial) algorithm.
- In these terms, finding a successful attack means finding a for which S(a,s) is true.
- Once someone proposes a possible attack, it take polynomial time to check whether this attack was successful.

# 3. Our explanation (cont-d)

- In other words:
  - if we consider "algorithms" including guessing steps such "algorithms" are known as non-deterministic algorithms,
  - then such a non-deterministic algorithm can solve the problem of finding a successful attack in polynomial time.
- The class of all the problems that can be solved by such nondeterministic polynomial time is usually denoted by NP.
- So, the problem of finding a successful attack belongs to the class NP.
- In NP-problems, the existence of a successful attack can be described as  $\exists a \, S(a, s)$ , i.e., as a formula with one existential quantifier.
- An existential quantifier is, in effect, an "or" (over all possible attacks), and in digital design, "or" is usually describe by a sum  $\Sigma$ .
- Thus, the class NP is also described as  $\Sigma_1 \mathbf{P}$ .

# 4. Our explanation (cont-d)

- On the other hand, finding a successful defense means finding s for which for every a, we have  $\neg S(a, s)$ .
- The formula describing the existence of such s is  $\exists s \, \forall a \, \neg S(a, s)$ .
- This formula also starts with  $\exists$ , but now it has two quantifiers, so the class of such formulas is denoted by  $\Sigma_2 \mathbf{P}$ .
- It is one of the classes next to  $\Sigma_1 \mathbf{P}$  in the so-called *polynomial hier-archy*.
- At present, it is not known whether problems from the class  $\Sigma_2 \mathbf{P}$  are, in general, more complex to solve that problems from  $\Sigma_1 \mathbf{P}$ .
- However, most computer scientists believe that, in general, problems  $\Sigma_2 \mathbf{P}$  are more complex.
- This explains why cyberattacks are easier than cyberdefense.

#### 5. Comment

- Why does not the same logic apply to the military attacks and defense?
- Because in cybersecurity success or failure of an attack depends on its ingenuity, brute force is a minor factor.
- In contrast, in military conflicts, the situation is different: there, brute force is an important often dominant factor.

### 6. References

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