

Quantum algorithms help to effectively detect symmetries and why it is important: a proposal

Jose Hernandez¹, Olga Kosheleva², and Vladik Kreinovich¹

Departments of ¹Computer Science and ²Teacher Education
University of Texas at El Paso, 500 W. University, El Paso, TX 79968, USA
jlhernandez24@miners.utep.edu, olgak@utep.edu, vladik@utep.edu

1. What are symmetries and why they are important

- One of the main objectives of science and engineering is:
 - to predict future events, and
 - to make sure that these future events are beneficial for us.
- Why are we able to predict future events?
- For example, why are we sure that if we drop a pen, it will fall down with an acceleration of 9.81 m/sec^2 ?
- Because this experiment was repeated many times:
 - at different locations on Earth,
 - at different orientations,
 - at different moments of time.
- And the result was always the same.
- In other words, when we shift in space or in time or rotate, the phenomenon remains the same.

2. What are symmetries and why they are important (cont-d)

- Similarly, why do we believe that Ohm's law will hold in the students' lab?
- Because this law held in many cases before.
- So it has been shown that the corresponding phenomena do not change under shifts and rotations.
- In physics, such transformations – under which the physical phenomena do not change – are known as *symmetries*.
- Symmetries do not have to be geometric.
- For example, if we change the sign of all electric charges, all phenomena remain the same.
- So the very possibility to predict future events is based on symmetries.

3. What are symmetries and why they are important (cont-d)

- In line with this, many new fundamental physical theories are now proposed:
 - not in terms of differential equations – as it was in Newton's time,
 - but by describing the corresponding symmetries.
- Differential equations follow from these symmetries.
- Moreover:
 - for many theories that were originally proposed in the form of differential equations, such as:
 - * Maxwell's equations for electrodynamics,
 - * Schroedinger's equations for quantum physics,
 - * Einstein's General Relativity equations describing space-time,
 - * and many others,
 - it is now known that these equations can be uniquely determined by the corresponding symmetries.

4. It is therefore important to detect symmetries in data

- Because of the above, the way to analyze a new phenomenon is to detect the corresponding symmetries.

5. Such a detection is not easy

- What is we use traditional – non-quantum – computers?
- Then, the only known algorithms for detecting symmetries :
 - require time which grows exponentially with data size,
 - which is thus not feasible:
 - e.g., for even a small size $n = 500$, already 2^{500} is larger than the lifetime of the Universe.
- This is true even in the simplest case, when:
 - we have a function f that maps bit sequences into bit sequences, and
 - symmetry means invariance under some shift.
- In precise terms: for some s , we have $f(x) = f(x \oplus s)$ for all x .
- Here, \oplus means component-wise addition modulo 2 (i.e., exclusive or).

6. Quantum computing can help

- In 1994, Daniel Simon provided a quantum algorithm that solves the above simple version of this problem in feasible time.
- This algorithm has been generalized to other possible symmetries.
- It helped Peter Shor come up with a feasible quantum algorithm for breaking:
 - the RSA encryption,
 - the main encryption that makes current communications secure.

7. What we propose

- Simon's algorithm originated in quantum computing.
- This is what motivated its generalizations.
- As we have described, symmetries are important in data analysis.
- So we propose to try to generalize Simon's results:
 - to physical situations beyond quantum computing,
 - namely, to situations when we are trying to make sense of the new data.

8. Acknowledgments

This work was supported in part:

- by the US National Science Foundation grants:
 - 1623190 (A Model of Change for Preparing a New Generation for Professional Practice in Computer Science),
 - HRD-1834620 and HRD-2034030 (CAHSI Includes),
 - EAR-2225395 (Center for Collective Impact in Earthquake Science C-CIES),
- by the AT&T Fellowship in Information Technology, and
- by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) Focus Program SPP 100+ 2388, Grant Nr. 501624329,